

Network Analysis Tools (NeAT) Tutorial

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Warning

This tutorial is in construction. The current version only covers a very small fraction of the *NeAT* tools. For the tools not covered yet by the tutorial, the DEMO buttons already give some hints about typical cases of utilization. We intend to develop further those tutorials very soon.

1 Introduction

Since a few years, large scale biological studies produced huge amounts of data about networks of molecular interactions (protein interactions, gene regulation, metabolic reactions, signal transduction). The integration of these data sets can be combined to acquire a global view of the pieces that, altogether, contribute to the complexity of biological processes. High-throughput data is however notoriously noisy and incomplete, and it is important to evaluate the quality of the different pieces of information that are taken in consideration for building higher views of biological networks.

An important effort will be required to extract reliable information from the ever-increasing ocean of high-throughput data. This will require the utilization of powerful tools that enable us to apply statistical analysis on large graphs. For this purpose, we developed the **Network Analysis Tools** (*NeAT*), as set of tools performing basic operations on networks and clusters.

The tools can be used in three ways:

1. **Web server interface**

<http://rsat.ulb.ac.be/neat/>

The Web interface gives a convenient and intuitive access to the tools, and allows you to bring your data sets through some typical analysis work flows in order to extract the best of it.

2. **Stand-alone application**

<http://rsat.ulb.ac.be/rsat/distrib/>

Most of the tools are freely available to academic users, according to a licence for non-commercial and non-military usage.

The license covers both the Regulatory Sequence Analysis Tools (*RSAT*) and the Network Analysis Tools (*NeAT*). It can be downloaded from the RSAT Web site.

3. **Web services**

In addition, people having computer skills can also use the same tools via a Web services interface, in order to integrate them in automatic work-flows. To obtain information on the Web services, connect the *NeAT* web server, and in the left menu, select **Information - Web services**.

2 Network visualization and format conversion

2.1 Introduction

2.1.1 Network visualization

To help the scientists apprehending their interest network, it is sometimes very useful to visualize them. Networks are generally represented by a set of dots (or of boxes) which represents its nodes that are linked via lines (the edges) or arrows (arcs in the case of directed graphs). The nodes and the edges may present a label and / or a weight. The node label is generally indicated in the node box and the edge label is often placed on the line.

NeAT contains some facilities to represent networks. It contains its own visualization software (display-graph) that will be described in the following. Moreover, it allows the conversion of the graph into formats that may be used by some visualisation tools like **Cytoscape** ([?], <http://www.cytoscape.org>), **yED** (<http://www.yworks.com/products/yed/>) or **VisANT** ([?], <http://visant.bu.edu/>).

Hereafter, we describe briefly some of the major formats used for graph description.

2.1.2 Graph formats

Incompatibility between file formats is a constant problem in bioinformatics. In order to facilitate the use of the NeAT website, most of our tools support several among the most popular formats used to describe networks.

- The tab-delimited format is a convenient and intuitive way to encode a graph. Each row represents an arc, and each column an attribute of this arc. The two columns fields are the source and target nodes. If the graph is directed, the source node is the node from which the arc leaves and the target node is the node to which the arc arrives. Logically, in undirected graph, the columns containing the source and the target node may be inverted. Some additional arc attributes (weight, label, color) can be placed in pre-defined columns. Orphan nodes can be included by specifying a source node without target. The tool **Pathfinder** extends this format by supporting any number of attributes on nodes or edges as well as the color, the label and the width of nodes and edges.
- A *GML* file is made up of nested key-value pairs. The most popular graph editors support GML as input format (like Cytoscape and yED). More information on this format can be found at <http://www.infosun.fim.uni-passau.de/Graphlet/GML/>.

- The *DOT* format is a plain text graph description language. DOT files can be loaded in the programs of the suite GraphViz (<http://www.graphviz.org/>). It is a simple way of describing graphs in a human- and computer-readable format. Similarly to GML, DOT supports various attributes on nodes (i.e. color, width, label).
- VisML is the XML format required by VisANT, a very light but powerful visualisation tool.
- Several tools also accept adjacency matrices as input. An adjacency matrix is a $N \times N$ table (with N the number of nodes), where a cell $A[i, j]$ indicates the weight of the edge between nodes i and j (or 1 if the graph is unweighted).

2.2 Visualisation of a co-expression network

2.2.1 Study case

In this demonstration, we will show you how to visualize a network using some popular network visualization tools. This network we will study consist in the top scoring edges of the yeast co-expression network included in the integrative database String [?]. This undirected weighted networks contains 537 nodes representing genes and 4801 edges. An edge between two nodes means that they are co-expressed. The weight expresses at which level both genes are co-expressed. We will explain how to display this network with NeAT, Cytoscape, yED and VisANT. As Cytoscape and yED are not online tools, we will only describe their utilization in the command-line section.

2.2.2 Protocol for the web server

Format conversion and layout calculation

1. In the *NeAT* menu, select the command **format conversion / layout calculation**.

In the right panel, you should now see a form entitled “convert-graph”.

2. Click on the link DEMO.

The form is now filled with a graph in the tab-delimited format, and the parameters have been set up to their appropriate value for the demonstration, i.e., the network will be converted from tab-delimited to GML format, the source node column is 1, the target column is 2 and the weight column is 3.

The option Calculate the layout of the nodes (only relevant for GML output may also be chosen, otherwise the nodes will all be in diagonal and the resulting graphic will not be very instructive.

If the edges present a weight, **convert-graph** is able to represent the weight of the edges by computing a color gradient proportional to edge weights and coloring the edges according to it. There are five different color gradients : blue, red, green, grey and yellow

to red. The darker (or the more colored) it is, the higher the weight. Moreover **convert-graph** can also change the width of the edge proportionally to its weight. To this, we must choose a color gradient for the Edge color intensity proportional to the weight and the option Edge width proportional to the weight of the edge must be checked (which is automatically the case with the demonstration).

3. Click on the button GO.

The resulting graph in GML format is available as an HTML link. Right click on the link and save it with name *string_coexpression.gml*.

Visualization using NeAT

1. In the Next Step pannel, click on Display the graph.

The form of **display-graph** is displayed. By default, the figure output format is jpeg, change it to png which gives a better resolution. NeAT also allow the postscript format.

2. Uncheck Calculate the layout of the nodes (mandatory for all input format except GML) as **convert-graph** already computed it.
3. Check Edge width proportional to the weight of the edges
4. Click on the GO button.

The figure is available by clicking on the HTML link. Clicking a the link leads to a static figure representing the network.

Visualization using VisANT

1. After the step *Format conversion and layout calculation*, click on the Load in VisANT

A page is displayed. Three links are available

- A link to the graph in the format you obtained it from **convert-graph** (here GML).
- A link (VisANT logo) to the VisANT applet
- A link to the graph in VisML (the input format of VisANT)

2. Click on the logo of VisANT

The VisANT applet is loaded.

3. Accept the authentication certifate.

2.2.3 Protocol for the command-line tools

Format conversion and layout calculation

If you have installed a stand-alone version of the NeAT distribution, you can use the programs **convert-graph** and **display-graph** on the command-line. This requires to be familiar with the Unix shell interface. If you don't have the stand-alone tools, you can skip this section and read the next section (Interpretation of the results). To visualize the networks with yED, VisANT or Cytoscape, you must of course install them on your computer.

1. First let us download the network file *string_coex_simple.tab* from the NeAT tutorial download page : http://rsat.ulb.ac.be/rsat/data/neat_tuto_data/
2. In this first step, we will convert the tab delimited String network that we just downloaded into a GML file by using this command. We compute the layout of the nodes. Moreover, we compute an edge width and an color proportional to the weight on the edge.

```
convert-graph -from tab -to gml -wcol 3 -i string_coex_simple.tab  
-o string_coex_simple.gml -layout -ewidth -wcol 3 -ecolors fire
```

Visualization using NeAT

Use the following command to create a graph using the NeAT **display-graph** program.

```
display-graph -in_format gml -out_format png -i string_coex_simple.gml  
-o string_coex_simple.png -ewidth
```

Visualization using Cytoscape (version 2.3)

1. Open Cytoscape
2. Click on File > Import > Network... > Select
3. Select the file *string_coex_simple.gml* If the graph contains more than 500 nodes, it will not be displayed immediately. Right click on the name of the graph file in the *Cytopanel 1* and select Create view....

Visualization using yED (version 3)

1. Open yED
2. Click on File > Import
3. Select the file *string_coex_simple.gml*

As NeAT GML converter add edge labels of the type *nodeName1_nodeName2* for un-weighted or unlabeled graph, you may need to remove the edge label for a better visibility.

4. Click on one edge (random)

The edge you clicked on is now selected.

5. Press *Ctrl+A*

All edges are now selected.

6. In the *Property view* (Right of the screen), in the *label* part, uncheck the *visible* option.

3 Comparisons between networks

3.1 Introduction

Protein interaction networks have deserved a special attention for molecular biologists, and several high-throughput methods have been developed during the last years, to reveal either pairwise interactions between proteins (two-hybrid technology) or protein complexes (methods relying on mass-spectrometry). The term *interactome* has been defined to denote the complete set of interactions between proteins of a given organism.

Interactome data is typically represented by an un-directed graph, where each node represents a polypeptide, and each edge an interaction between two polypeptides.

The yeast interactome was characterized by the two-hybrid method by two independent groups, Uetz and co-workers [?], and Ito and co-workers [?], respectively. Surprisingly, the two graphs resulting from these experiments showed a very small intersection.

In this tutorial, we will use the program ***compare-graphs*** to analyze the interactome graphs published by from Uetz and Ito, respectively.

We will first perform a detailed comparison, by merging the two graphs, and labelling each node according to the fact that it was found in Ito's network, in Uetz' network, or in both. We will then compute some statistics to estimate the significance of the intersection between the two interactome graphs.

3.2 Computing the intersection, union and differences between two graphs

3.2.1 Study case

In this demonstration, we will compare the networks resulting from the two first publications reporting a complete characterization of the yeast interactome, obtained using the two-hybrid method. The first network [?] contains 865 interactions between 926 proteins. The second network [?] contains 786 interactions between 779 proteins. We will merge the two networks (i.e. compute their union), and label each edge according to the fact that it is found in Ito's network, Uetz' network, or both. We will also compute the statistical significance of the intersection between the two networks.

3.2.2 Protocol for the web server

1. In the *NeAT* menu, select the command ***network comparison***.

In the right panel, you should now see a form entitled “compare-graphs”.

2. Click on the button DEMO.

The form is now filled with two graphs, and the parameters have been set up to their appropriate value for the demonstration. At the top of the form, you can read some information about the goal of the demo, and the source of the data.

3. Click on the button GO.

The computation should take a few seconds only. The result page shows you some statistics about the comparison (see interpretation below), and a link pointing to the full result file.

4. Click on the link to see the full result file.

3.2.3 Protocol for the command-line tools

If you have installed a stand-alone version of the NeAT distribution, you can use the program **compare-graphs** on the command-line. This requires to be familiar with the Unix shell interface. If you don't have the stand-alone tools, you can skip this section and read the next section (Interpretation of the results).

We will now describe the use of **compare-graphs** as a command line tool. The two two-hybrid datasets described in the previous section may be downloaded at the following address http://rsat.ulb.ac.be/rsat/data/neat_tuto_data/. These are the files *uetz_2001.tab* and *ito_2002.tab*.

1. Go in the directory where the files containing the graphs to compare are located.
2. Type the following command

```
compare-graphs -v 1 -Q ito_2002.tab -R uetz_2001.tab -return union \  
-o uetz_2001_union_ito_2002.tab
```

Using these options, some comparison statistics are displayed and the results are stored in the tab-delimited file *uetz_2001_union_ito_2002.tab*.

In order to compute the difference or the intersection, you must change the `-return` option. For example, to compute the intersection, you should type.

```
compare-graphs -v 1 -Q ito_2002.tab -R uetz_2001.tab -return intersection \  
-o uetz_2001_inter_ito_2002.tab
```

3.2.4 Interpretation of the results

The program **compare-graphs** uses symbols R and Q respectively, to denote the two graphs to be compared. Usually, R stands for reference, and Q for query.

In our case, R indicates Ito's network, whereas Q indicates Uetz' network. The two input graphs are considered equivalent, there is no reason to consider one of them as reference, but this does not really matter, because the statistics used for the comparison are symmetrical, as we will see below.

Union, intersection and differences

The result file contains the union graph, in tab-delimited format. This format is very convenient for inspecting the result, and for importing it into statistical packages (R, Excel, ...).

The rows starting with a semicolon (;) are comment lines. They provide you with some information (e.g. statistics about the intersection), but they will be ignored by graph-reading programs. The description of the result graph comes immediately after these comment lines.

Each row corresponds to one arc, and each column specifies one attribute of the arc.

1. **source**: the ID of the source node
2. **target**: the ID of the target node
3. **label**: the label of the arc. As labels, we selected the option “Weights on the query and reference”. Since the input graphs were un-weighted, edge labels will be used instead of weights. The label <NULL> indicates that an edge is absent from one input network.
4. **color** and **status**: the status of the arc indicates whether it is found at the intersection, or in one graph only. A color code reflects this status, as indicated below.
 - *R.and.Q*: arcs found at the intersection between graphs *R* and *Q*. Default color: green.
 - *R.not.Q*: arcs found in graph *R* but not in graph *Q*. Default color: violet.
 - *Q.not.R*: arcs found in graph *Q* but not in graph *R*. Default color: red.

The result file contains several thousands of arcs, and we will of course not inspect them by reading each row of this file. Instead, we can generate a drawing in order to obtain an intuitive perception of the graph.

Sizes of the union, intersection and differences

The beginning of the result file gives us some information about the size of the two input files, their union, intersection, and differences.

| | | | | |
|----------------------------|-------|------|---------------------|--|
| ; Counts of nodes and arcs | | | | |
| ; Graph | Nodes | Arcs | Description | |
| ; R | 779 | 786 | Reference graph | |
| ; Q | 926 | 865 | Query graph | |
| ; QvR | 1359 | 1529 | Union | |
| ; Q^R | 346 | 122 | Intersection | |
| ; Q!R | 580 | 743 | Query not reference | |
| ; R!Q | 433 | 664 | Reference not query | |

Statistical significance of the intersection between two graphs

The next lines of the result file give some statistics about the intersection between the two graphs. These statistics are computed in terms of arcs.

| | | | |
|--|----------|-----------------------------------|--------------------------------------|
| ; Significance of the number of arcs at the intersection | | | |
| ; Symbol | Value | Description | Formula |
| ; N | 1359 | Nodes in the union | |
| ; M | 922761 | Max number of arcs in the union | $M = N \cdot (N-1) / 2$ |
| ; $E(Q^R)$ | 0.74 | Expected arcs in the intersection | $E(Q^R) = Q \cdot R / M$ |
| ; Q^R | 122 | Observed arcs in the intersection | |
| ; perc_Q | 14.10 | Percentage of query arcs | $\text{perc_Q} = 100 \cdot Q^R / Q$ |
| ; perc_R | 15.52 | Percentage of reference arcs | $\text{perc_R} = 100 \cdot Q^R / R$ |
| ; Jac_sim | 0.0798 | Jaccard coefficient of similarity | $\text{Jac_sim} = Q^R / (Q \vee R)$ |
| ; Pval | 2.5e-228 | P-value of the intersection | $\text{Pval} = P(X \geq Q^R)$ |

A first interesting point is the maximal number of arcs (M) that can be traced between any two nodes of the union graph. In our study case, the graph obtained by merging Ito's and Uetz' data contains $N = 1359$ nodes. This graph is un-directed, and there are no self-loops. The maximal number of arcs is thus $M = N \cdot (N - 1) / 2 = 922,761$. This number seems huge, compared to the number of arcs observed in either Uetz' ($A_Q = 865$) or Ito's ($A_R = 786$) graphs. This means that these two graphs are sparse: only a very small fraction of the node pairs are linked by an arc.

The next question is to evaluate the statistical significance of the intersection between the two graphs. For this, we can already compute the size that would be expected if we select two random sets of arcs of the same sizes as above ($A_Q = 865$, $A_R = 4,038$).

If the same numbers of arcs were picked up at random in the union graph, we could estimate the probability for an arc to be found in the network R as follows: $P(R) = A_R / M = 0.000852$. Similarly, the probability for an arc of the union graph to be part of the network Q is $P(Q) = A_Q / M = 0.000937$. The probability for an arc to be found independently in two random networks of the same sizes as R and Q is the product of these probabilities.

$$P(QR) = P(Q) \cdot P(R) = A_R / M \cdot A_Q / M = 7.98e - 07$$

The number of arcs expected by chance in the intersection is the probability multiplied by the maximal number of arcs.

$$\begin{aligned}
 E(QR) &= P(QR) \cdot M \\
 &= (A_Q \cdot A_R) / M \\
 &= 7.98e - 07 \cdot 922761 = 0.74
 \end{aligned}$$

Thus, at the intersection between two random sets of interaction, we would expect on the average a bit less than one interaction. It seems thus clear that the 122 interactions found at the intersection between the two published experiments is much higher than the random expectation.

We can even go one step further, and compute the *P-value* of this intersection, i.e. the probability to select at least that many interactions by chance.

The probability to observe *exactly* x arcs at the intersection is given by the hypergeometrical distribution.

$$P(QR = x) = \frac{C_R^x C_{M-R}^{Q-x}}{C_M^Q} \quad (3.1)$$

where

R is the number of arcs in the reference graph;

Q is the number of arcs in the query graph;

M is the maximal number of arcs;

x is the number of arcs at the intersection between the two graphs.

By summing this formula, we obtain the P-value of the intersection, i.e. the probability to observe *at least* x arcs at the intersection.

$$Pval = P(QR \geq x) = \sum_{i=x}^{\min(Q,R)} P(X = i) = \sum_{i=x}^{\min(Q,R)} \frac{C_R^i C_{M-R}^{Q-i}}{C_M^Q}$$

We can replace the symbols by the numbers of our study case.

$$\begin{aligned} Pval &= P(QR \geq 122) \\ &= \sum_{i=122}^{\min(865,786)} \frac{C_{786}^i C_{922761-786}^{865-i}}{C_{922761}^{865}} \\ &= 2.5e-228 \end{aligned}$$

This probability is so small that it comes close to the limit of precision of our program ($\approx 10^{-321}$).

Summary

In summary, the comparison revealed that the number of arcs found in common between the two datasets (Ito and Uetz) is highly significant, despite the apparently small percentage of the respective graphs it represents (14.10% of Ito, and 15.52% of Uetz).

3.3 Strengths and weaknesses of the approach

3.4 Exercises

1. Using the tool the tool **network randomization**, generate two random graphs of 1000 nodes and 1000 arcs each (you will need to store these random networks on your hard drive). Use the tool **network comparison** to compare the two random graphs. Discuss the result, including the following questions:
 - a) What is the size of the intersection ? Does it correspond to the expected value ?
 - b) Which P-value do you obtain ? How do you interpret this P-value ?
2. Randomize Ito's network with the tool **network randomization**, and compare this randomized graph with Uetz' network. Discuss the result in the same way as for the previous exercise.

3.5 Troubleshooting

1. The P-value of the intersection between two graphs is 0. Does it mean that it is impossible to have such an intersection by chance alone ?

No. Any intersection that you observe in practice might occur by chance, but the limit of precision for the hypergeometric P-value is $\approx 10^{-321}$. Thus, a value of 0 can be interpreted as $Pval < 10^{-321}$.

2. The web server indicates that the result will appear, and after a few minutes my browser displays a message "No response the server".

How big are the two graphs that you are comparing ? In principle, compare-graphs can treat large graphs in a short time, but if your graphs are very large (e.g. several hundreds of thousands of arcs), the processing time may exceed the patience of your browser. In such case, you should consider either to install the stand-alone version of **NeAT** on your computer, or write a script that uses **NeAT** via their Web services interface.

4 Node degree statistics

4.1 Introduction

In a graph, the degree k of a node is the number of edges connected to this node. If the graph is directed, we can make a distinction between the in-degree (the number input arcs) and the out-degree (number of output arcs). In this case, the degree of the node consists in the sum of the in-degree and of the out-degree of this node.

Different nodes having different degrees, this variability is characterized by the degree distribution function $P(k)$, which gives the probability that a node has exactly k edges, or, in other words gives the observed frequency of a node of degree k .

Scale-free graphs were first described by Barabasi based on the study of the web connectivity, followed by several different biological networks [?].

A graph is scale-free if the distribution of the vertex degree (k) follows a power-law distribution of the form $P(k) k^{-\gamma}$.

The main property of such graphs is that it should have on one hand some highly connected nodes, called hubs, which are central to the network topology, and *keep the network together* and on the other hand a lot of poorly connected nodes linked to the hubs.

In the following, we will check if this scale free property also applies to the two-hybrid network described by Uetz *et al* [?] by computing the degree of each node and plotting the node degree distribution of the graph.

4.2 Analysis of the node degree distribution of a biological network

4.2.1 Study case

In this demonstration, we will analyze the node degree distribution of the first published yeast protein interaction network. This network is the first attempt to study the yeast interactome using the two-hybrid method and contains 865 interactions between 926 proteins [?].

4.2.2 Protocol for the web server

1. In the *NeAT* menu, select the command ***node topology statistics***.

In the right panel, you should now see a form entitled “graph-topology”.

2. Click on the button DEMO.

The form is now filled with a graph in the tab-delimited format, and the parameters have been set up to their appropriate value for the demonstration, i.e., the degree of all nodes will be computed. At the top of the form, you can read some information about the goal of the demo, and the source of the data.

As this is a protein - protein interaction graph, we can consider that an interaction between a protein A with a protein B corresponds to an interaction between protein B and protein A. The graph is thus not directed.

You can uncheck the computation of the closeness and betweenness as these statistics will not be discussed in this section and as this process will increase the computation time.

3. Click on the button GO.

The computation should take less than one minute. On one hand, the result page displays a link to the result file and on the other hand the graphics and raw data of the node degree distribution are also available. These will be discussed in the *Interpretation of the results* section.

4.2.3 Protocol for the command-line tools

If you have installed a stand-alone version of the NeAT distribution, you can use the program **graph-topology** on the command-line. This requires to be familiar with the Unix shell interface. If you don't have the stand-alone tools, you can skip this section and read the next section (Interpretation of the results).

We will now describe the use of **graph-topology** as a command line tool. The two two-hybrid dataset described in the previous section may be downloaded at the following address http://rsat.ulb.ac.be/rsat/data/neat_tuto_data/. This is the file *uetz_2001.tab*.

1. The first step consist in applying **graph-topology** on the two-hybrid dataset. To this, go into the directory where you downloaded the file *uetz_2001.tab* and use this command.

```
graph-topology -v 1 -i uetz_2001.tab -return degree -all \  
-o uetz_2001_degrees.tab
```

The file *uetz_2001_degrees.tab* is created and contains the degree of each node of the Uetz *et al* data set.

2. In the second step, we will study the degree distribution of the nodes. To this, we use the program **classfreq** from the RSAT suite that compute the distribution of a set of number. As the graph we are working with is undirected, we will only compute this degree distribution for the global degree of the nodes which is the second column of the file *uetz_2001_degrees.tab* obtained in the previous step.

```
classfreq -i uetz_2001_degrees.tab -v 1 -col 2 -ci 1 \  
-o uetz_2001_degrees_freq.tab
```

3. Finally, we will display the distribution graph in the PNG format in order to visualize the degree distribution and determine if it has a scale free behaviour. The program XYgraph from RSA-tools will be used for this purpose. Note that we could use other tools like **Microsoft Excel** or **R**. The results will be stored in the file *uetz_2001_degrees_freq.png* that you can open with any visualization tool.

```
XYgraph -i uetz_2001_degrees_freq.tab \  
-title 'Global node degree distribution (interaction graph: Uetz 2001)' \  
-xcol 2 -ycol 4,6 -xleg1 Degree -lines \  
-yleg1 'Number of nodes' -legend -header -format png \  
-o uetz_2001_degrees_freq.png
```

4.2.4 Interpretation of the results

graph-topology result file

Open the resulting file produced by **graph-topology**. According to the requested level of verbosity (`-v #` option), the file begins with some lines starting with the '#' or ';' symbols that contains some information about the graph and the description of the columns.

The results consists in a two columns data set.

1. Node name
2. Global degree

Note that if you used the '-directed' option, the resulting file contains 3 more columns specifying the in-degree, the out-degree and whether the node is only a source node or a target node.

Node degree distribution

Let us first have a look at the node degree distribution data file produced by the **classfreq** program (raw data). This file is a tab-delimited file containing 9 columns. Each line consists in a value interval. In our case, the value is the degree of the nodes.

1. Minimal value of the interval
2. Maximal value of the interval
3. Central value of the interval
4. Frequency : Number of elements in this class interval (number of nodes having a degree comprised between the minimal and the maximal values.
5. Cumulative frequency.
6. Inverse cumulative frequency

7. Relative frequency : number of elements in this class over the total number of elements
8. Relative cumulative frequency
9. Inverse relative cumulative frequency

The first result line contains the distribution results for the nodes having only one neighbour (i.e. degree comprised between 1 and 2), from it we can see that 577 over 926, i.e., 62% of the nodes have a degree of one. Moreover, about 90% of the nodes have a degree lower than 4. This is indicative of the scale-free nature of the interaction network.

The figure best illustrates the scale-freeness of the graph. When looking at the graphical representation of this distribution, we can see two curves. The blue curve represents the absolute frequency and the green curve the inverse cumulative frequency. The exponential decrease of both curves shows that there are a lot more nodes poorly connected than highly connected (hubs). The Uetz graph thus presents a scale free behaviour.

chapterStudy of the neighborhood of the nodes

4.3 Introduction

In a graph, the neighbours of a node consist in the set of nodes that are connected to this node up to a certain distance, i.e., the number of steps between the source node and its neighbours. In weighted graphs, one can also consider the neighbours up to a certain maximal weight.

In the following, we will refer to the node for which we search the neighbours the *seed node*.

According to the type of graph, it might be interesting to retrieve the neighbours of the nodes in a graph.

For example, in protein-protein interaction network, the function of the neighbours of a protein whose biological role is unknown might give insights in the function of the protein. Moreover, in interaction graphs, if a group of neighbours have similar biological functions, they are likely to form a structural complex.

In co-regulation networks, where each node is a gene and an edge between two genes means that those genes are co-regulated (i.e. co-repressed and co-expressed), exploring the neighbours of the nodes may help in the discovery of new regulons.

In the following, we will illustrate the study of nodes neighborhood by looking for neighbours of some orphan proteins (i.e. protein of unknown function) in a protein protein interaction network. We will then look if the neighbours of these proteins present similar functions.

4.4 Analysis of the neighbours of orphan nodes in an interaction protein network

4.4.1 Study case

In this demonstration, we will analyze the neighbours of the orphan nodes of the Gavin *et al* (2006) interaction data set. These interaction data were obtained by co-immunoprecipitation

followed by a mass spectrometry experiment in order to discover structural protein complexes. [?]. This network contains 6531 interactions between 1430 proteins.

We will then compare these groups of neighbours with functional classes of proteins annotated in the MIPS [?] in order to detect if the groups of neighbours present a significantly high number of co-regulated proteins.

4.4.2 Protocol for the web server

1. In the *NeAT* menu, select the command **get node neighborhood**. In the right panel, you should now see a form entitled “graph-neighbours”.
2. Open a connection to the demo dataset download web page.
http://rsat.ulb.ac.be/rsat/data/neat_tuto_data/
3. Download the files *gavin_2006_names.tab*, *orphan_gavin.tab* and *mips_name_class_description.tab* on your computer.
4. In the *Upload graph from file* text area, load the file *gavin_2006_names.tab* you just downloaded.
5. Uncheck `Include each node in its neighborhood (with a distance of zero)`
6. Check the radio-button *Node selection* in the seed node part of the form
7. In the *Upload seed nodes from file* text area, load the file *orphan_gavin.tab* you just downloaded.
8. Click on the button GO.

The computation should take less than one minute.

The result page should display the results in the tab-delimited or HTML format. These files will be described in the section *Interpretation of the results*

9. We will now see if the different groups of neighbours contain a significantly high number of proteins of similar function. To this, we will compare the groups of neighbours we just obtained with annotated groups of proteins, e.g., the genes annotated according to the gene ontology [?] or, in this example, according to the functional classes of the MIPS [?]. In the *Next step* panel, click on the button *Compare the groups of neighbours*.

You are redirected to the form of another program **compare-classes** that allows to compare two class files (the query file and the reference file). Each class of a query file is compared to each class of a reference file. The number of common elements is reported, as well as the probability to observe at least this number of common elements by chance alone. The query classes are already loaded and consist in the different groups of neighbours we discovered previously with **graph-neighbours**.

10. In the *Upload reference classes from file* text area, load the file *mips_name_class_description.tab* downloaded in the first part of this tutorial. The classes files are two column files, the first column contains the elements and the second column the class to which the elements belong. Elements may belong to more than one class.
11. The default parameters are sufficient. We will only keep the comparison presenting a significance higher than 0.
12. Click on the button GO.
13. You obtain the links to the result file in the tab-delimited format or in the HTML format. The obtained results will be described in the next section.

4.4.3 Protocol for the command-line tools

If you have installed a stand-alone version of the NeAT distribution, you can use the program **graph-neighbours** on the command-line. This requires to be familiar with the Unix shell interface. If you don't have the stand-alone tools, you can skip this section and read the next section (Interpretation of the results).

We will now describe the use of **graph-neighbours** as a command line tool. The Gavin *et al* (2006) [?] co-immunoprecipitation dataset described in the previous section and the other files necessary for this tutorial may be downloaded at the following address

http://rsat.ulb.ac.be/rsat/data/neat_tuto_data/
(*gavin_2006_names.tab*, *orphan_gavin.tab* and *mips_name_class_description.tab*).

1. The first step consist in applying **graph-neighbours** on the co-immunoprecipitation dataset. To this, go into the directory where you downloaded the files *gavin_2006_names.tab*, *orphan_gavin.tab* and use this command.

```
graph-neighbours -v 1 -i gavin_2006_names.tab \
  -seedf orphan_gavin.tab \
  -o gavin_2006_orphan_neighbours_1.tab
```

The file *gavin_2006_orphan_neighbours_1.tab* is created and contains for each node of the seed file the list of its direct neighbours, i.e., for each protein, the list of proteins that co-precipitated with it.

2. In the second step, we will compare these groups of neighbours to different groups of annotated proteins in order to discover if the groups of neighbours do contain a significantly high number of proteins of similar functions. This will give insights into the function of the orphans proteins used as seed nodes in the first step. To this, we will use the RSAT **compare-classes** program that allows to compare two class files (the query file and the reference file) (see previous section or the RSAT tutorial for a more complete description of **compare-classes**). Use the following command to compare the two files.


```
compare-classes -v 1 \  
-q gavin_2006_orphan_neighbours_1.tab \  
-r mips_name_class_description.tab \  
-lth sig 0 -sort sig -return proba,occ,jac_sim \  
-o gavin_2006_orphan_neighbours_1_cc_mips_functionnal_classes.tab
```

We obtain a file *gavin_2006_orphan_neighbours_1_cc_mips_functionnal_classes.tab* containing the significant comparison results. We will discuss it in the following section (interpretation of the results).

4.4.4 Interpretation of the results

graph-neighbours result file

According to the requested level of verbosity, the result file may first contain several lines (starting with “#” or “;”). These deliver some information about the analysed graph (number of nodes, edges, seed nodes, ...). The results are then displayed in four columns.

1. Name of the neighbour.
2. Name of the seed node (for which the neighbours are sought in the graph).
3. Distance between the seed node and its neighbour (number of steps).
4. The last column, only relevant for directed graph, indicate whether the arc between the seed node and its neighbour is an out- or an in-going arc.

This file can be considered as a class file (see above for a more complete description) with the name of the neighbour being the member (first column) and the name of the seed node, the name of the class (second column).

compare-classes result file

The result of the comparison between the groups of neighbours and the MIPS annotated classes are displayed in a multi-column file sorted by decreasing order of significance. When looking at the HTML version of the file, you may click on the header on the column to sort the table according to this field.

Each line displays the comparison between a MIPS annotated class (reference class) and a group of neighbours (query class). What we want to know is if there is a significantly high number of members of the same MIPS class in a given group of neighbours.

ref Name of the MIPS fonctionnal class.

query Name of the group of neighbours (seed node).

R Size of the reference class (number of members in this MIPS class).

- Q Size of the query class (number of neighbour for this seed node).
- QR Intersection size between the group of neighbours and the fonctionnal class.
- QvR Union size between the group of neighbours and the fonctionnal class.
- R!Q Elements that are in the fonctionnal class but not in the groups of neighbours.
- Q!R Elements that are not in the fonctionnal class but are in the groups of neighbours.
- !Q!R Elements that are not in the fonctionnal class nor in the groups of neighbours.
- P-val P-value of the comparaison, propability (according to the hypergeometric law) to be wrong when claimin that there is a significatively high number of proteins of the same class in the group of neighbours.
- E-val E-value of the comparaison. P-value multiplied by the total number of comparaisons. This value corresponds to the estimated number of false positives for a given P-value threshold.
- sig Significance of the comparaison. This correpsonds to $-\log_{10}(E - val)$. This index gives an intuitive perception of the exceptionality of the common elements : a negative significance indicates that the common matches are likely to come by chance alone, a positive value that they are significant.

Considering the file, we can observe that 7 seed nodes (on the 46) have a group of neighbours presenting a similar function. For example, 9 out of the 10 neighbours of the Yil161w protein (interacting with this protein) have their function related to ribosome biogenesis and 8 out of 10 neighbours are located in the cytoplasm. This may indicate that this protein may also be implied in ribosome biogenesis

5 Graph clustering

5.1 Introduction

Abruptly, graph clustering consists in grouping the nodes of the networks into different classes or clusters. The groupment of the nodes can be done according to various different criteria, i.e., nodes of the same color, nodes of the same type, etc. Commonly, nodes are grouped according to the fact they present a relatively high number of connections between them compared to the number of connections with the other nodes composing the network. In the following, we will only consider clustering methods aiming at retrieving highly interconnected groups of nodes in a network.

In bioinformatics, a lot of clustering approaches have already been applied to various types of network, e.g. protein-protein interaction network (see among others [?, ?, ?]), metabolic graphs [?], biological sequences ([?, ?]), etc.

Clustering of protein interaction network may be of valuable help in order to retrieve in a large graphs real biological complexes in the cell. Moreover, if in the detected complexes some of proteins are of unknown function but the rest of the proteins present all present a similar function, this may give insights in the function of the unknown protein.

In the following, we will apply different graph based clustering approaches on the yeast protein - protein interaction network published by Gavin *et al* [?] and obtained by multiple co-immunoprecipitation experiments with each yeast protein used as bait followed by a mass spectrometry procedure to identify all the proteins that precipitated with the baits.

The clustering algorithms we will apply are the **MCL** [?, ?] and **RNSC** [?]. Hereafter, follows a short description of both clustering algorithms copied from [?].

The Markov Cluster algorithm (**MCL**) simulates a flow on the graph by calculating successive powers of the associated adjacency matrix. At each iteration, an *inflation step* is applied to enhance the contrast between regions of strong or weak flow in the graph. The process converges towards a partition of the graph, with a set of high-flow regions (the clusters) separated by boundaries with no flow. The value of the *inflation parameter* strongly influences the number of clusters.

The second algorithm, Restricted Neighborhood Search Clustering (**RNSC**), is a cost-based local search algorithm that explores the solution space to minimize a cost function, calculated according to the numbers of intra-cluster and inter-cluster edges. Starting from an initial random solution, **RNSC** iteratively moves a vertex from one cluster to another if this move reduces the general cost. When a (user-specified) number of moves has been reached without decreasing the cost function, the program ends up.

In order to dispose of a negative control, we advice the reader to read the next chapter about graph randomization and alteration.

5.2 Network clustering comparison

5.2.1 Study case

In this demonstration, we will compare the performances of two graph based clustering algorithms **MCL** and **RNSC**. First, we will apply them to the protein - protein interaction described by Gavin *et al* [?], secondly we will compare the resulting clusters to the complexes annotated for the yeast in the MIPS database [?].

Note that as the interaction network and the MIPS complexes are different dataset (i.e. different proteins), the performances of the algorithm will be rather low.

To run this tutorial on the command line, you need to have both **RNSC** and **MCL** installed on your computer. You can find the MCL source code on <http://micans.org/mcl/> and **RNSC** on http://rsat.ulb.ac.be/rsat/rnsc/rnsc_rewritten_compiled32.zip.

5.2.2 Protocol for the web server

Dataset download

Go on the NeAT demo dataset web page (http://rsat.ulb.ac.be/rsat/data/neat_tuto_data/) and download the MIPS complexes (*mips_complexes.tab*).

Network clustering with MCL

1. In the *NeAT* left menu, select the command **graph-based clustering (MCL)**.

In the right panel, you should now see a form entitled “MCL”.

2. Click on the button DEMO.

The form is now filled with the Gavin co-immunoprecipitation protein interaction network graph in the tab-delimited format, and the parameters have been set up to their appropriate value for the demonstration, i.e., the inflation value (the MCL main parameter) is set to 1.8, the optimal value for **MCL** protein interaction network clustering [?].

The inflation acts mainly on the number of clusters resulting from the clustering, i.e., by increasing the inflation, you will obtain a larger number of smaller clusters.

Note that MCL accepts weighted networks (which is not the case here), a higher weight on an edge will reinforce the strength of the link between two nodes.

3. Click on the button GO.

The computation should take less than one minute. On one hand, the result page displays a link to the result file and on the other hand a graphic showing the size distribution of the obtained complexes is also available. These will be discussed in the *Interpretation of the results* section.

4. Save the resulting file under the name *gavin_2006_mcl_inf_1.8_clusters.tab* by right clicking on the resulting file and choosing *Save as*

Network clustering with RNSC

1. In the *NeAT* left menu, select the command ***graph-based clustering (RNSC)***.

In the right panel, you should now see a form entitled “RNSC”.

2. Click on the button DEMO.

The form is now filled with the Gavin co-immunoprecipitation protein interaction network graph in the tab-delimited format, and the parameters have been set up to their appropriate value for the demonstration, i.e., the numerous RNSC parameters are set to the optimal values for ***RNSC*** protein interaction network clustering determined in [?]. However, in this study, we found that the ***RNSC*** performances were not strongly affected by the parameters values.

Note that, unlike MCL, RNSC does not accept weighted networks.

3. Click on the button GO.

The computation should take less than one minute. On one hand, the result page displays a link to the result file and on the other hand a graphic showing the size distribution of the obtained complexes is also available. These will be discussed in the *Interpretation of the results* section.

4. Save the resulting file under the name *gavin_2006_rnsc_clusters.tab* by right clicking on the resulting file and choosing *Save as*

Clustering quality assessment

In the following, we will only describe the procedure to quantify the performances of the clustering algorithms by comparing the ***MCL*** obtained clusters to the complexes annotated in the MIPS database. You will thus have to redo this whole section with the ***RNSC*** clustering results.

1. In the *NeAT* left menu, select the command ***Compare classes/clusters***.

In the right panel, you should now see a form entitled “compare-classes”. This program will build a contingency table, i.e., a table where each line represents the annotated complexes and each column the clusters of highly connected proteins. This matrix will then be used to compute quality statistics.

2. In the “Upload query classes from file” menu, select the file *gavin_2006_mcl_inf_1.8_clusters.tab* we just computed.
3. In the “Upload reference classes from file” menu, select the file *mips_complexes.tab* we just downloaded.

4. Select “Matrix file” as output format
5. Click on the button GO.
6. The contingency table (see the resulting links as text or HTML file) can now be used in the next process by clicking on the button `contingency table statistics`.

In the right panel, you should now see a form entitled “contingency-stats”. This program will compute the statistics described in [?], namely the *PPV*, the *sensitivity* and the *Separation* statistics in order to estimate the quality of a clustering results to predict the complexes annotated in the MIPS.

7. Click on the button GO.

The resulting statistics will be described in the following section *Interpretation of the results*, save them under the name `gavin_2006_mcl_inf_1.8_vs_mips_stats.tab`.

Re-do the whole procedure with the file obtained with **RNSC** and save the contingency-stats output under the name `gavin_2006_rnsc_vs_mips_stats.tab`.

5.2.3 Protocol for the command-line tools

If you have installed a stand-alone version of the NeAT distribution, you can also use all the programs on the command-line. This requires to be familiar with the Unix shell interface. If you do not have the stand-alone tools, you can skip this section and read the next section (*Interpretation of the results*).

The explanation of the parameters used for **RNSC** and **MCL** in this approach are described in the *Web server* section of this chapter.

We will now describe the use of **RNSC**, **MCL**, **compare-classes**, **convert-classes**, **convert-graph** and **contingency-stats** as command line tools. As a preliminary step, go on the NeAT demo dataset web page (http://rsat.ulb.ac.be/rsat/data/neat_tuto_data/) and download the MIPS complexes (`mips_complexes_names.tab`) and the Gavin interaction dataset (`gavin_2006_names.tab`).

Network clustering with MCL

1. The first step consist in applying **MCL** on the co-immunoprecipitation dataset. To this, go into the directory where you downloaded the file `uetz_2001.tab` and use this command.

```
mcl gavin_2006_names.tab -I 1.8 --abc -o gavin_2006_mcl_inf_1.8_clusters.mcl
```

The file `gavin_2006_mcl_inf_1.8_clusters.mcl` is created and contains the clusters of highly connected node in the interaction dataset. However, this file is formatted in the **MCL** format that is not usable by the NeAT / RSAT tools. We will thus use the program **convert-classes** to convert this file in a tab delimited format with the following command.

```
convert-classes -i gavin_2006_mcl_inf_1.8_clusters.mcl \
-o gavin_2006_mcl_inf_1.8_clusters.tab \
-from mcl -to tab
```

The resulting file is a two column file containing for each node (first column) the cluster to which it belongs (second column).

Network clustering with RNSC

1. The first step will consist in converting the tab delimited format in which the protein interaction dataset is encoded into a format readable by the RNSC clustering algorithm. To this, we will use the `convert-graph` program with the following command.

```
convert-graph -from tab -to rnscl \
-i gavin_2006_names.tab -o gavin_2006_rnsc
```

Two files are created, *gavin_2006_rnsc.rnsc* and *gavin_2006_rnsc_node_names.rnsc*. The first one contains the graph in itself, under the format of an adjacency list. However, each node is identified by a number. The protein names corresponding to the nodes identifiers are encoded in the second file (two column tab delimited file).

2. We can now apply **RNSC** on the network with the following command.

```
rnsc -g gavin_2006_rnsc.rnsc -t 50 -T 1 -n 15 -N 15 -e 3 -D 50 \
-d 3 -o gavin_2006_rnsc_clusters.rnsc
```

The file *gavin_2006_rnsc_clusters.rnsc* is created and contains the clusters of highly connected node in the interaction dataset. However, this file is formatted in the **RNSC** format that is not usable by the *NeAT* / *RSAT* tools. We will thus use the program **convert-classes** to convert this file in a tab delimited format with the following command.

```
convert-classes -i gavin_2006_rnsc_clusters.rnsc \
-o gavin_2006_rnsc_clusters.tab \
-from rnsc -to tab \
-names gavin_2006_rnsc_node_names.rnsc
```

The resulting file is a two column file containing for each node (first column) the cluster to which it belongs (second column).

Assessing clustering quality

In this section, we will describe how to build a contingency table by comparing the clusters extracted from the networks by **MCL** and **RNSC** to annotated complexes and the way to compute statistics on this contingency-table.

We will only describe the procedure for the **MCL** results. You should redo this section for the **RNSC** clustering results.

1. The program **compare-classes** can build (among other things) a contingency table, i.e., a table where each line represents the annotated complexes and each column the clusters of highly connected proteins. This table will then be used to compute quality statistics.

```
compare-classes -q gavin_2006_inf_1.8.tab \
                -r mips_complexes_names.tab -matrix QR \
                -o gavin_2006_inf_1.8_cc_complexes_matrix.tab
```

The file *gavin_2006_inf_1.8_cc_complexes_matrix.tab* now contains a contingency table in a tab delimited format.

2. We can now study the quality of the clustering with the **contingency-stats** tool that was used in [?] to compute standard evaluation statistics like the *PPV*, sensitivity and the accuracy that will be precisely described in the following.

```
contingency-stats -i gavin_2006_inf_1.8_cc_complexes_matrix.tab \
                  -o gavin\_2006\_mcl\_inf\_1.8\_vs\_mips\_stats.tab
```

Re-do this section with the *gavin_2006_rnsc_clusters.rnsc* to obtain a file called *gavin_2006_rnsc_*

5.2.4 Interpretation of the results

Files description

Contingency table As already explained in a previous section, having n MIPS complexes and m clusters, the contingency table T is a $n \cdot m$ matrix where row i corresponds to the i^{th} annotated complex, and column j to the j^{th} cluster. The value of a cell $T_{i,j}$ indicates the number of proteins found in common between complex i and cluster j .

The clustering quality will be evaluated from this table by calculating the Sensitivity (Sn), the Positive predictive value (PPV), the row wise separation (Sep_r) and the cluster separation (Sep_c).

Contingency table metrics A list of metrics and their value. These will be described in the next section.

Metrics description

Sensitivity, Positive predictive value and geometric accuracy For each complex, we can calculate a sensitivity value. This corresponds to the maximal fraction of protein of a complex that are attributed by a clustering algorithm to the same cluster. Sn measures how well proteins belonging to the same complex are grouped within the same cluster.

$$Sn_i = \frac{\max_i(T_{ij})}{N_i}$$

where N_i corresponds to the size of the complex.

Moreover, for each cluster j , we calculated the Positive Predictive Value (PPV) which corresponds to the maximal fraction of a cluster belonging to the same complex. This reflects the ability of this cluster to detect one complex.

$$PPV_j = \frac{\max_j(T_{ij})}{M_j}$$

where M_j corresponds to the cluster size.

To summarize these values at the level of the confusion table, we calculated the average of these values. First, we calculated their classical mean by averaging all the PPV_j and Sn_i values. We also calculated a weighted mean where the clusters and complexes have a weight proportional to their relative size on the calculation of the mean.

$$\begin{aligned} Sn &= \frac{\sum_{i=1}^n Sn_i}{n} \\ PPV &= \frac{\sum_{j=1}^m PPV_j}{m} \\ Sn_w &= \frac{\sum_{i=1}^n N_i Sn_i}{\sum_{i=1}^n N_i} \\ PPV_w &= \frac{\sum_{j=1}^m M_j PPV_j}{\sum_{j=1}^m M_j} \end{aligned}$$

Sensitivity and PPV reflect two contradictory tendencies of the clustering. Sn increases when all the proteins of the same complex are grouped in the same cluster and PPV decreases when proteins coming from different complexes are grouped in the same cluster. If all the proteins of the network are grouped in the same cluster, we maximize the Sn but the PPV is almost 0. On the other hand, if each protein is placed in a different cluster, the PPV is maximized but the sensitivity is very low. A compromise must be found between these two cases by using another statistics. We defined the geometric accuracy as the geometrical mean of the PPV and the Sn .

$$Acc_g = \sqrt{PPV \cdot Sn}$$

Separation We also defined another metrics called *Separation (Sep)*. High *Sep* values indicated a high bidirectionnal correspondance between a cluster and a complex.

The row-wise separation estimates how a complex is isolated from the others. Its maximal value is 1 if this correspondance is perfect, i.e., when all the protein of a complex are grouped in one cluster and if this cluster does not contain any other protein. This maximal value may also be reached when the complex is separated between many clusters containing only members of the complex.

$$Sep_{r_i} = \sum_{j=1}^m \left(\frac{T_{i,j}}{\sum_{j=1}^m T_{i,j}} \cdot \frac{T_{i,j}}{\sum_{i=1}^n T_{i,j}} \right)$$

The column-wise separation indicates how well a cluster isolates one or more complex from the other clusters. The maximal value 1 indicates that a cluster contains all the elements of one or more complexes.

$$Sep_{c_j} = \sum_{i=1}^n \left(\frac{T_{i,j}}{\sum_{j=1}^m T_{i,j}} \cdot \frac{T_{i,j}}{\sum_{i=1}^n T_{i,j}} \right)$$

As for the sensitivity and the *PPV*, for each clustering result, all values of Sep_{c_j} and Sep_{r_i} are averaged over all clusters and all complexes. We then calculate a global separation value by calculating the geometrical mean of the average row wise separation and of the average column wise separation.

$$Sep = \sqrt{Sep_c \cdot Sep_r}$$

Score comparaison

In the following, we can observe the statistics described in the previous paragraph computed for the clustering results of **RNSC** and **MCL**.

We can observe that **MCL** seems to produce slightly more valuable results as

1. The unweighted sensitivity is a bit higher for **MCL** than for **RNSC** and the weighted sensitivity is much higher.
2. The *PPV* is a only bit lower for **MCL** than for **RNSC**.

These results might certainly be explained by the large number of clusters found by **RNSC** compared to **MCL**. Indeed, the *PPV* increases and the sensitivity decreases with the number of a clusters. We can observe the same tendencies for the other metrics.

3. Global metrics (accuracy and separation) are generally higher for **MCL** than for **RNSC**

| metrics | RNSC | MCL |
|---------|--------|--------|
| ncol | 470 | 189 |
| nrow | 220 | 220 |
| min | 0 | 0 |
| max | 18 | 27 |
| mean | 0.0086 | 0.0214 |
| sum | 889 | 889 |
| Sn | 0.603 | 0.652 |
| PPV | 0.424 | 0.472 |
| acc | 0.513 | 0.562 |
| acc_g | 0.505 | 0.555 |
| Sn_w | 0.622 | 0.767 |
| PPV_w | 0.642 | 0.549 |
| acc_w | 0.632 | 0.658 |
| acc_g_w | 0.632 | 0.649 |
| sep | 0.303 | 0.353 |
| sep_c | 0.207 | 0.381 |
| sep_r | 0.443 | 0.327 |

Remark: The following table was generated using the RSAT program ***compare-scores***, see the help of this command line tool for more information

6 Influence of graph alteration and randomization on clustering

6.1 Introduction

Although negative controls and method evaluation are crucial points to the experimental biologist, this is far from being the same in bioinformatics where, too often, no negative control is associated to the predictions, so that one cannot estimate the probability of these predictions to be biologically valid.

For this reason, in NeAT we developed programs allowing to randomize and to add some specified levels of noise to networks. This allows the user to apply the techniques used to find relevant results on networks where there is less or no signal and thus where no interesting result should emerge.

NeAT programs are able to generate randomized networks according to three methods.

1. *Node degree conservation* : this approach consists in shuffling the edges, each node keeping the same number of neighbors as in the original graph.
2. *Node degree distribution conservation* : in which the global distribution of the node degree is conserved but each node presents a different degree than in the original graph.
3. *Erdos-Renyi randomization* : where edges are distributed between pairs of nodes with equal probability.

6.2 Quantitative assessment of a clustering algorithm

6.2.1 Study case

In this demonstration, we will use the approach developed in [?] where we evaluated the performances of different graph clustering algorithms. Graph clustering algorithms allow to retrieve in a graph the groups of nodes that contain more connections between them than with the rest of the nodes of the graph. Clustering algorithms are often used in biology in order to extract coherent groups of nodes from networks (complexes detection (e.g. see [?, ?, ?, ?]), protein families detection [?], co-expressed genes detection in co-expression networks (e.g see [?]), ...). The NeAT web server proposes the **MCL** (*Markov Cluster algorithm*) clustering algorithm developed by Stijn van Dongen [?, ?]. To follow the command-line tools instructions, you should have MCL installed on your computer (available at <http://micans.org/mcl/>).

MCL simulates a flow on the graph by calculating successive powers of the associated adjacency matrix. At each iteration, an *inflation step* is applied to enhance the contrast between regions of strong or weak flow in the graph. The process converges towards a partition of the graph, with a set of high-flow regions (the clusters) separated by boundaries with no flow. The value of the *inflation parameter* strongly influences the number of clusters. According to [?], the optimal inflation value for clustering protein interaction networks is 1.8.

We will use an artificial interaction network created from the complexes annotated in the MIPS database by creating an edge between all the nodes belonging to the same complex [?]. This network contains 12262 edges between 1095 nodes. We will then use the MCL clustering algorithm on this network, on a little altered network, on a highly altered network and finally on a randomized network.

We will then compare these clusters to the MIPS complexes and estimate how well MCL can retrieve protein complexes from a protein-protein interaction and the influence of the noise on the results.

In this example, we will only use random alteration, i.e., the edges that are removed are randomly chosen. This is done to mimick what happens really in biological experiments where some inter-relationships between the nodes (genes, proteins, metabolites, ...) may not be discovered (false negatives) or are erroneously discovered (false positives). However the **alter-graph** program also allows to alterate the network with targeted attack on user-selected nodes. In their study, Spirin and Mirny [?] showed the affect of node targeted attacks on clustering results.

6.2.2 Protocol for the web server

Dataset download

Go on the demo dataset web page http://rsat.ulb.ac.be/rsat/data/neat_tuto_data/ and download the MIPS complex network file (*complexes_rm_00_ad_00.tab*) and the complexes (*mips_complexes.tab*).

Network alteration

1. In the *NeAT* menu, select the command **network alteration**.
2. In the *Upload graph from file* text area, load the file *complexes_rm_00_ad_00.tab* containing the MIPS complexes network that you just downloaded.
3. In the *edges to add* text area, enter 10%.
4. In the *edges to remove* text area, enter 10%.
5. Click on the button GO.
6. Right click on the resulting file and save it with name *complexes_rm_10_ad_10.tab*.

Re-do the this alteration procedure using 50% of edges removal and 100% of edges addition. Save the resulting file with name *complexes_rm_50_ad_100.tab*.

Network randomization

1. In the *NeAT* menu, select the command **network randomization**.
2. In the *Upload graph from file* text area, load the file *complexes_rm_00_ad_00.tab*.
3. Select the Node degree conservation randomization type.
4. Click on the button GO.
5. Right click on the resulting file and save with name *complexes_rm_00_ad_00_random.tab*.

Networks clustering and clustering assessment

1. In the *NeAT* menu, select the command **graph-based clustering MCL**.
2. In the *Upload graph from file* text area, load the file *complexes_rm_00_ad_00.tab*.
3. Click on the button GO. You should now obtain a link to the clustering results and the distribution of the sizes of the different clusters.
4. In the *Next step* panel, click on the button *Compare these clusters to other clusters*.
5. In the *Upload reference classes from file* text area, load the *mips_complexes.tab* file.
6. Choose the *matrix file* output format
7. Click on the button GO. You now obtain a contingency table, i.e, a table with N rows and M columns (N being the number of MIPS complexes and M , the number of clusters). Each cell contains the number of protein common to one complex and one cluster.
8. To calculate some statistics on this contingency table, click on the *contingency-table statistics* button in the *Next step* panel.
9. The **contingency-stats** form appears. As the contingency table is already uploaded, just click on the GO button.
10. Save the resulting file under name *contingency_stats_rm_00_ad_00.tab*

Repeat these steps for *complexes_rm_10_ad_10.tab*, *complexes_rm_50_ad_100.tab* and *complexes_rm_00_ad_00_random.tab* and save the resulting files under the names *contingency_stats_ad_10_rm_100.tab*, *contingency_stats_ad_50_rm_100.tab*, *contingency_stats_ad_00_rm_00_random.tab*, respectively.

6.2.3 Protocol for the command-line tools

If you have installed a stand-alone version of the NeAT distribution, you can use the programs **random-graph** and **alter-graph** on the command-line. This requires to be familiar with the Unix shell interface. If you don't have the stand-alone tools, you can skip this section and read the next section (Interpretation of the results).

We will now describe the use of **random-graph**, **alter-graph**, **compare-classes** and **contingency-stats** as command line tools. For this tutorial, you need to have the MCL program installed.

Start by going on the demo dataset download web page http://rsat.ulb.ac.be/rsat/data/neat_t and downloading the MIPS complex network file (*complexes_rm_00_ad_00.tab*) and the complexes (*mips_complexes.tab*).

Network alteration

1. Go in the directory where you downloaded the file.
2. Use the following commands to alter the graph. Note that MCL is not an RSAT / NeAT program and thus cannot treat RSAT comments lines (starting with “#” or with “;”). We thus have to suppress them in the command.

```
alter-graph -v 1 -i complexes_rm_00_ad_00.tab \  
-rm_edges 10% -add_edges 10% \  
| cut -f 1,2 | grep -v ';' > complexes_rm_10_ad_10.tab
```

Re-use this command, but modify the percentage of removed (-rm_edges 50%) and added edges (-add_edges 100%). Save the resulting file with name *complexes_rm_50_ad_100.tab*.

Network randomization

1. Use the following commands to randomize the graph by shuffling the edges. The node degrees will be conserved.

```
random-graph -v 1 -i complexes_rm_00_ad_00.tab \  
-random_type node_degree \  
| cut -f 1,2 | grep -v ';' > complexes_rm_00_ad_00_random.tab
```

Networks clustering and clustering assessment

1. Use the following commands to apply MCL on the network

```
mcl complexes_rm_00_ad_00.tab \  
--abc -I 1.8 -o complexes_rm_00_ad_00_clusters.mcl
```

2. Convert the cluster file obtained with MCL with the program **convert-classes** into a file that is readable by NeAT / RSAT (two column cluster file).

```
convert-classes -i complexes_rm_00_ad_00_clusters.mcl
-from mcl -to tab -o complexes_rm_00_ad_00_clusters.tab
```

3. Compare the obtained clusters to the MIPS complexes with the program ***compare-classes***

```
compare-classes -q complexes_rm_00_ad_00_clusters.tab \
-r mips_complexes.tab \
-matrix QR \
-o complexes_rm_00_ad_00_clusters_cc_complexes_matrix.tab
```

4. Study the obtained matrix with the ***contingency-stats*** program

```
contingency-stats -i complexes_rm_00_ad_00_clusters_cc_complexes_matrix.tab \
-o contingency_stats_ad_00_rm_00.tab
```

Repeat these steps for *complexes_rm_10_ad_10.tab*, *complexes_rm_50_ad_100.tab* and *complexes_rm_00_ad_00_random.tab* and save the resulting files under the names *contingency_stats_ad_00_rm_10.tab*, *contingency_stats_ad_50_rm_100.tab*, *contingency_stats_ad_00_rm_00_random.tab*, respectively.

6.2.4 Interpretation of the results

We will now compare the performances of MCL when applied to networks containing an increasing proportion of noise or no signal at all.

Files description

Randomized network As the real MIPS complexes network, this randomized network contains 12262 edges between 1095 nodes. With our parameter choice, no edge should be duplicated. However, as in ***random-graph*** the iterative process designed to avoid duplicated edges may not be totally efficient, some duplicated edges may subsist in the randomized network.

Altered networks This file is a classical NeAT tab-delimited edge list. However, there is a fifth column that indicates whether the edge comes from the original graph (*original*) or was added randomly (*random*).

- As the MIPS complex newtwork, the network with 10% of added and removed edges contains 12262 edges between 1095 nodes, which is logical as we removed and added the same number of edge (in this case 1226).
- The network with 100% of added edges (+ 12262 edges) and 50% of removed edges (- 6131 edges) contains 18393 edges between 1095 nodes. This graph contains thus more noisy than relevant edges.

Contingency table See the previous chapter (Graph clustering) for a complete description of a contingency table.

Contingency table metrics A list of metrics and their value. These will be described in the next section.

Metrics description

Sensitivity, Positive predictive value and geometric accuracy See the previous chapter (Graph clustering) for a complete description of a contingency table.

Score comparison

The table summarizes the kind of values that should be obtained for the metrics described in the previous section. As the alteration and the randomization procedure are random processes, you should not obtain exactly the same results.

| # | true | ad10 / rm10 | ad100 / rm50 | random |
|----------------|--------|-------------|--------------|--------|
| <i>ncol</i> | 125 | 114 | 713 | 361 |
| <i>nrow</i> | 220 | 220 | 220 | 220 |
| <i>mean</i> | 0.0569 | 0.0624 | 0.00998 | 0.0197 |
| <i>Sn</i> | 0.998 | 0.985 | 0.418 | 0.291 |
| <i>PPV</i> | 0.884 | 0.836 | 0.867 | 0.459 |
| <i>acc</i> | 0.941 | 0.91 | 0.642 | 0.375 |
| <i>acc_g</i> | 0.939 | 0.907 | 0.602 | 0.365 |
| <i>Sn_w</i> | 0.997 | 0.992 | 0.502 | 0.157 |
| <i>PPV_w</i> | 0.621 | 0.62 | 0.688 | 0.244 |
| <i>acc_g_w</i> | 0.787 | 0.785 | 0.588 | 0.196 |
| <i>sep_r</i> | 0.567 | 0.507 | 0.676 | 0.192 |
| <i>sep_c</i> | 0.998 | 0.979 | 0.208 | 0.117 |
| <i>sep</i> | 0.752 | 0.704 | 0.375 | 0.15 |

As expected, the value of the global parameters, the geometric accuracy (row *acc_g*), the weighted geometric accuracy (row *acc_g_w*) and the separation (row *sep*) decrease drastically as the network contain less and less relevant information.

We can observe that the sensitivity is more affected than the *PPV* and that the complex wise separation (*sep_r*) is more affected than the cluster wise separation. This is due to the fact that by increasing the noise, MCL increases the number of small sized clusters (*ncol*) too and, as we saw in previous section, this has an impact on the sensitivity.

Note that with a random graph, we would have a separation of 0.15 but an unweighted geometric accuracy of 0.365 which is far from being 0. The relatively good performances of MCL on the highly altered graph must thus be taken with caution as the gain in performances is only of 23%. This illustrates the interest of using negative controls.

7 Path finding

7.1 Introduction

Given a biological network and two nodes of interest, the aim of k shortest path finding is to enumerate the requested number of shortest paths connecting these nodes ordered according to their weight. For instance, we might look for all shortest paths between a receptor and a DNA binding protein to predict a signal transduction pathway from a protein protein interaction network. Another example is the prediction of a metabolic pathway given two reactions or compounds of interest and a metabolic network.

A problem encountered in many biological networks is the presence of so-called hub nodes, that is nodes with a large number of connections. For example, in bacterial protein-protein interaction networks, CRP has the role of a hub node because it interacts with many targets. Likewise, in metabolic networks, compounds such as ADP or water are hubs, since they are generated and consumed by thousands of reactions.

The shortest path very likely traverses the hub nodes of a network. It depends on the biological context, whether this behaviour is desired or not. In metabolic networks, we are less interested in paths going through water or ADP, since those paths are often not biological relevant. For instance, we can bypass the glycolysis pathway by connecting glucose via ADP to 3-Phosphoglycerate. To avoid finding irrelevant pathways like this one, we tested different strategies and concluded that using a weighted network gave the best results [?],[?]. In a weighted network, not the shortest, but the lightest paths are searched. Hub nodes receive large weights, making them less likely to appear in a solution path.

Whether weights are used and how they are set has to be decided depending on the biological network of interest.

In this chapter, we will demonstrate path finding on the example of metabolic networks. We will work on a network assembled from all metabolic pathways annotated for the yeast *S. cerevisiae* in BioCyc (Release 10.6) [?]. We will also show the influence of the weighting scheme on path finding results.

7.2 Computing the k shortest paths in weighted networks

7.2.1 Study case

The yeast network constructed from BioCyc data consists of 1,185 nodes and 2,656 edges. It has been obtained by unifying 171 metabolic pathways. Note that this network is bipartite,

which means that it is made up of two different node types: reactions and compounds. An edge never connects two nodes of the same type. For the tutorial, we choose to represent the metabolic data as undirected network. Note that higher accuracies can be achieved by representing metabolic data by directed networks that contain for each reaction its direct and reverse direction, which are treated as mutually exclusive. See the advanced options of the Pathfinder tool for mutual exclusion of reactions in directed metabolic networks.

We will recover the heme biosynthesis II pathway given its start and end compound, namely glycine and protoheme. First, we will use the "degree" weighting scheme, which penalizes hub nodes. Second, we will infer the path using the "unit" weighting scheme and compare the results.

7.2.2 Protocol for the web server

1. In the *NeAT* menu, select the command ***k shortest path finding***.

In the right panel, you should now see a form entitled "Pathfinder".

2. Click on the button DEMO1.

The form is now filled with the BioCyc demo network, and the parameters have been set up to their appropriate value for the demonstration. At the top of the form, you can read some information about the goal of the demo, and the source of the data.

3. Click on the button GO.

The computation should take no more than two minutes. When it is finished, a link to the results should appear.

4. Click on the link to see the full result file.

It lists a table of all paths found for the requested rank number (5 by default). You can also specify another type of output, for instance a network made up of all paths found. Vary the parameter `Output type` for this.

To see how results change with modified weight, you can repeat steps 1 and 2. Before clicking on GO, choose "unit weight" as `Weighting scheme` and set the Rank to 1. Continue as described above. You will obtain another paths table than before.

7.2.3 Protocol for the command-line tools

This section assumes that you have installed the RSAT/NeAT command line tools.

You can find the demo network `Scer_biocyc.tab` in `$RSAT/public_html/demo_files`.

Type the following command to enumerate paths up to the 5th rank in the weighted network:

```
java -Xmx800m graphtools.algorithms.Pathfinder -g Scer_biocyc.tab -f tab -s gly -t protohem
```

To find paths in the unweighted network, type:

```
java -Xmx800m graphtools.algorithms.Pathfinder -g Scer_biocyc.tab -f tab -s gly -t protohem
```

7.2.4 Interpretation of the results

Degree weighting scheme

First, we run Pathfinder with degree weighting scheme, which is the default weighting scheme of the demo. This weighting scheme sets the weights of compound nodes to their degree and of reaction nodes to one. The first ranked path obtained should look like this:

GLY 5-AMINOLEVULINIC-ACID-SYNTHASE-RXN 5-AMINO-LEVULINATE PORPHOBILSY RXN PORPHOBILINOGEN OHMETHYLBILANESYN-RXN HYDROXYMETHYLBILANE UROGENIIISYN-RXN UROPORPHYRINOGEN-III UROGENDECARBOX-RXN COPRO-PORPHYRINOGEN_III RXN0-1461 PROTOPORPHYRINOGEN PROTOPORGENOXI-RXN PROTOPORPHYRIN_IX PROTOHEMEFERROCHELAT-RXN **PROTOHEME**

This path recovers very well the annotated heme biosynthesis II pathway.

Unit weighting scheme

We repeated path finding on the same network but used the unit weighting scheme, which sets all node weights to one. This is equivalent to path finding in an unweighted network. We obtain a large number of paths of first rank, among them this one:

GLY GLUTATHIONE-SYN-RXN ADP PEPDEPHOS-RXN PROTON PROTOHEMEFERROCHEL RXN **PROTOHEME**

This path deviates strongly from the heme biosynthesis II pathway annotated in BioCyc. It contains two hub nodes: ADP and PROTON.

7.3 Summary

To sum up: path finding can predict pathways with high accuracy if an appropriate weighting scheme is applied to the network of interest. Our metabolic example shows that the heme biosynthesis II pathway is accurately predicted when using a weighted network and not found at all when using an unweighted network. The take home message is that in order to use Pathfinder on biological networks, weights have to be carefully adjusted.

7.4 Strengths and Weaknesses of the approach

7.4.1 Strengths

The strength of the approach is that for a given network and appropriate weighting scheme, pathways can be discovered with high accuracy. These pathways may be known or novel pathways. Other methods such as pathway mapping are unable to recover entirely novel pathways or pathways which are combinations of known pathways.

7.4.2 Weaknesses

The weakness is that the weighting scheme has to be optimized for the biological network of interest.

7.5 Troubleshooting

1. No path could be found.

Make sure that your start and end nodes are present in your network of interest. If no path could be found, none of the end nodes is reachable from the start nodes, thus no path exists. For big graphs and long waiting time, there is the possibility that the pre-processing step of REA, namely to compute the shortest paths from the source to all nodes with Dijkstra, was not finished before the server timeout. In this case, a path might exist but could not be detected due to the timeout.

2. An out of memory error occurred.

When searching for paths with the "unit" weighting scheme in large networks, there might be a large number of possible paths for each requested rank. Although REA has a memory-efficient way to store paths with pointers, there is a limit for the number of paths that can be hold in memory. Reduce the number of requested paths or the size of the graph or use another weighting scheme.

8 Metabolic path finding

8.1 Introduction

The metabolic pathfinder enumerates metabolic pathways between a set of start nodes and a set of end nodes, where start and end nodes may be compounds, reactions or enzymes (which are mapped to the reactions they catalyze). When choosing the right parameters (which are set by default), the metabolic pathways found are with high probability biochemically relevant.

The accuracy of path finding in metabolic networks (as in other biological networks) is diminished by the presence of hub nodes (highly connected compounds such as ATP, NADPH or CO₂) in the network. Path finding algorithms will traverse the network preferentially via the hub nodes, thereby inferring biochemically irrelevant pathways. Different strategies have been devised to overcome this problem. Arita introduced the mapping and tracing of atoms from substrates to products [?]. This strategy is also applied in the Pathway Hunter Tool available at <http://pht.tu-bs.de/PHT/>. Other tools rely on rules to avoid hub nodes, e.g. the pathway prediction system at UMBBD (<http://umbbd.msi.umn.edu/predict/>). Didier Croes et al. used weighted graphs to avoid highly connected nodes [?],[?]. The functionality of Didier Croes' tool is covered by the metabolic pathfinder (with the weighted reaction network).

Metabolic pathfinder relies on a mixed strategy: On the one hand, it makes use of weighted graphs to avoid irrelevant hub nodes and on the other hand, it integrates KEGG RPAIR annotation [?] to favor for each traversed reaction main over side compounds. KEGG RPAIR is a database that divides reactions into reactant pairs (substrate-product pairs) and classifies the reactant pairs according to their role in the reaction. For instance, the cofactor reactant pair A00001 couples NADP⁺ with NADPH. Main reactant pairs connect main compounds and should be traversed preferentially by path finding algorithms.

The KEGG RPAIR annotation is integrated by construction of the undirected RPAIR network, which consists of 7,058 reactant pairs, 4,297 compounds and 14,116 edges for KEGG version 41.0. Alternatively, two other networks are available: the directed reaction network evaluated in [?] and an undirected reaction-specific RPAIR network, in which each reaction is divided in its reactant pairs.

Note that in more recent KEGG versions, identifiers of reactant pairs start with RP instead of A.

In this chapter, we will recover the aldosterone pathway using the RPAIR and the reaction

network respectively. Note that the study case was carried out with data from KEGG LIGAND version 41.0. Results might differ for more recent KEGG versions.

8.2 Enumerating metabolic pathways between compounds, reactions or enzymes

8.2.1 Study case

Aldosterone is a human steroid hormone involved in the regulation of ion uptake in the kidney and of blood pressure. It is synthesized from progesterone. We aim to recover the aldosterone biosynthesis pathway by providing its start and end reaction.

8.2.2 Protocol for the web server

1. In the *NeAT* menu, select the entry **Metabolic path finding**.

In the right panel, you should now see a form entitled “Metabolic pathfinder”.

2. Click on the button DEMO2 located at the bottom of the form.

The metabolic pathfinder form is now filled with the start and end reaction of the aldosterone biosynthesis pathway. In addition, information on this pathway is displayed.

3. Click on the button GO.

4. The seed node selection table appears.

This table lists for each reaction the reactant pair identifier(s) associated to it. Note that reaction R02724 is associated to two reactant pairs.

The seed node selection form allows you to select the correct among all compounds matching your query string in case you provided a partial compound name. If you give KEGG compound identifiers, it displays the name of each compound. For EC numbers, it lists associated reactions or reactant pairs. The seed node selection form also warns you in case you provide problematic identifiers.

5. Click on the button GO.

The computation should take no more than one minute.

Then, a table is displayed, which lists the found paths in the order of their weight. The table may be sorted according to other criteria by clicking the respective column header. Each path node is linked to its corresponding KEGG entry for easy inspection of results.

If you set `Output format` in the metabolic pathfinder form to “Graph”, you obtain an image of the inferred pathway generated by the program **dot** of the graphviz tool suite and a link to the pathway in the selected graph format.

To see how results change with the choice of the graph, you can repeat steps 1 and 2. In the metabolic path finding form, select Reaction graph instead of RPAIR graph (which is selected by default) and follow step 3 to 5. You will notice in the seed node selection form that the reaction identifiers are no longer mapped to reactant pairs.

8.2.3 Protocol for the command-line tools

This section assumes that you have installed the RSAT/NeAT command line tools.

The metabolic pathfinder is a web application on top of Pathfinder. You may run metabolic path finding on command line by launching the Pathfinder command line tool on the RPAIR and reaction networks, which are provided in the KEGG graph repository reachable from the metabolic pathfinder manual page.

Type the following command in one line to find paths in the RPAIR network:

```
java -Xmx800m graphtools.algorithms.Pathfinder -g RPAIRGraph_allRPAIRs_undirected.t
-s 'A02437' -t 'A02894' -b -y rpairs
```

To repeat path finding in the reaction network, type in one line:

```
java -Xmx800m graphtools.algorithms.Pathfinder -g ReactionGraph_directed.txt -d -f
-s 'R02724>/R02724<' -t 'R03263>/R03263<' -b -y con
```

8.2.4 Interpretation of the results

Metabolic path finding in the RPAIR network

The path of first rank does not reproduce exactly the annotated pathway. Instead, it suggests a deviation via 21-hydroxypregnenolone, bypassing progesterone. This path might be a valid alternative, as it appears on the KEGG map for C21-Steroid hormone metabolism in human. One of the two second-ranked paths corresponds to the annotated pathway.

First ranked path:

A02437 (1.14.15.6) Pregnenolone A03407 (1.14.99.10) 21-Hydroxypregnenolone A00731 (1.1.1.145, 5.3.3.1) 11-Deoxycorticosterone A03469 (1.14.15.4) Corticosterone A02893 (1.14.15.5) 18-Hydroxycorticosterone **A02894**

Second ranked paths:

A02437 (1.14.15.6) Pregnenolone A00386 (1.1.1.145, 5.3.3.1) Progesterone A02045 (1.14.99.10) 11-Deoxycorticosterone A03469 (1.14.15.4) Corticosterone A02893 (1.14.15.5) 18-Hydroxycorticosterone **A02894**

A02437 (1.14.15.6) Pregnenolone A00386 (1.1.1.145, 5.3.3.1) Progesterone A02047 (1.14.15.4) 11beta-Hydroxyprogesterone A03467 (1.14.99.10) Corticosterone A02893 (1.14.15.5) 18-Hydroxycorticosterone **A02894**

Metabolic path finding in the reaction network

The paths of first and second rank traverse a side compound, namely adrenal ferredoxin. None of these paths is therefore biochemically valid. In the weighted reaction graph all highly connected side compounds such as ATP and water are avoided. However, adrenal ferredoxin is a rare side compound, thus weighting is not sufficient to bypass it.

First ranked path:

R02724< Reduced adrenal ferredoxin R03262> 18-Hydroxycorticosterone **R03263**>

Second ranked paths:

R02724> Oxidized adrenal ferredoxin R02726< Reduced adrenal ferredoxin R03262> 18-Hydroxycorticosterone **R03263**>

R02724> Oxidized adrenal ferredoxin R02725< Reduced adrenal ferredoxin R03262> 18-Hydroxycorticosterone **R03263**>

8.3 Summary

Metabolic path finder provides k shortest path finding in metabolic networks constructed from KEGG LIGAND and KEGG RPAIR. The metabolic path finder is coupled with a mirror of the KEGG database to allow quick identification of partial compound names and to annotate results.

8.4 Strengths and Weaknesses of the approach

8.4.1 Strengths

The metabolic path finder has the following benefits compared to other metabolic path finding tools:

1. It has been extensively evaluated on 55 reference pathways from three organisms.
2. It supports compounds, reactions, reactant pairs and EC numbers as seed nodes.
3. It can handle sets of start and end nodes.

8.4.2 Weaknesses

The metabolic path finding tool has the following weaknesses:

1. RPAIR does not cover all compounds in KEGG. Thus, the RPAIR network is less comprehensive than the reaction network.

2. By default, the metabolic path finder cannot infer directions of reactions in pathways because of the way the networks were constructed (being undirected or treating all reactions as reversible). However, custom metabolic networks may contain irreversible reactions and it is therefore possible to infer directed pathways from custom networks.
3. The metabolic path finder can only partly infer cyclic pathways or pathways in which the same enzymes act repeatedly on a growing chain.

8.5 Troubleshooting

1. A **Parameter error** occurred.

By default, the optimal parameter values are set. However, if you set your own values, they might not be in the supported value range. Check the Metabolic path finder manual.

2. The seed node selection form displays the message: "You provided invalid identifier(s)!"

This occurs when you provide identifiers that do not match any KEGG identifier, EC number or KEGG compound name. Check your identifiers or in case you provided a compound name, check whether the compound is present in KEGG.

3. The seed node selection form displays the message: "The given compound is not part of the sub-reaction graph."

As stated in the Weaknesses section, the RPAIR network does not contain all KEGG compounds due to incomplete coverage of the RPAIR database. Try to search paths for this compound in the reaction network.

4. No path could be found.

This may happen in the RPAIR network because in this network reactant pairs belonging to the same reaction exclude each other. Try the reaction-specific RPAIR network or the reaction network instead.

5. An out of memory error occurred.

This may occur when requesting a large number of paths with the reactant subreaction and compound weighting schemes set to unweighted. In general, when setting the weighting schemes to unweighted, biochemically irrelevant paths will be returned. Use another weighting scheme or reduce the number of requested paths to avoid this error.

9 KEGG network provider

9.1 Introduction

KEGG network provider allows you to extract metabolic networks from KEGG [?] that are specific to a set of organisms. In addition, you can exclude certain compounds or reactions from these networks.

A range of tools works with KGML files. Click on “Manual -> Related tools” to see a selection of them. KEGG network provider differs from these tools by allowing also the extraction of RPAIR networks and by supporting filtering of compounds, reactions and RPAIR classes.

KEGG network provider itself has no network analysis or visualization functions, but you can use a NeAT tool (a choice of them will appear upon termination of network construction) or any other graph analysis tool that reads gml, VisML or dot format for these purposes.

For visualization of KEGG networks, you can use iPATH [?], KGML-ED [?] or metaSHARK [?]. Yanasquare [?] and Pathway Hunter Tool [?] offer organism-specific KEGG network construction in combination with analysis functions. With [?], you can construct KEGG metabolic networks in R.

It should be noted that KEGG annotators omitted side compounds in the KGML files. Thus, certain molecules (such as CO₂, ATP or ADP) might be absent from the metabolic networks extracted from these files.

It is also worth noting that constructing metabolic networks from KGML files produces networks of much lower quality than those obtained by manual metabolic reconstruction. In manual reconstruction, several resources are taken into account, such as the biochemical literature, databases and genome annotations (e.g. [?]). This is why the metabolism of only a few organisms has been manually reconstructed so far.

In automatically reconstructed networks, reactions might not be balanced and compounds might occur more than once with different identifiers (see e.g. [?] for annotation problems in KEGG). For the purpose of path finding the automatically reconstructed metabolic networks may still be of interest.

9.2 Construction of yeast and E. coli metabolic networks

9.2.1 Study case

Our study case consists in the construction of two metabolic networks: one for five yeast species and the other for *Escherichia coli K-12 MG1655*. We will compare path finding results obtained for these two networks for a metabolic reference pathway (Lysine biosynthesis).

9.2.2 Protocol for the web server

1. In the *NeAT* menu, select the entry **Download organism-specific networks from KEGG**. In the right panel, you should now see a form entitled “KEGG network provider”.
2. Click on the button DEMO located at the bottom of the form.

The KEGG network provider form has now loaded the organism identifiers of five yeast species. As explained in the form, the species concerned are: *Saccharomyces bayanus*, *Saccharomyces mikatae*, *Saccharomyces paradoxus*, *Schizosaccharomyces pombe* and *Saccharomyces cerevisiae*.
3. Click the checkbox `directed network` to construct a directed metabolic network.
4. Click on the button GO.

The network extraction should take only a few seconds. Then, a link to the extracted network is displayed. In addition (for formats *tab-delimited* and *gml*), the Next step panel should appear.
5. Click on the button “Find metabolic paths in this graph” in the Next step panel. This button opens the Metabolic pathfinder with the yeast network pre-loaded.
6. Enter C00049 (L-Aspartate) as source node and C00047 (L-Lysine) as target node.
7. In section **Path finding options**, set the rank to 1. We are only interested in the first rank.
8. In section **Output**, select Graph as output with “paths unified into one graph”
9. Click GO. The seed node selection form appears to confirm our seed node choice.
10. Click GO. After no more than one minute of computation, the graph unifying first rank paths between L-aspartate and L-lysine should appear. You can store the graph image on your machine for later comparison.

Repeat the previous steps, but instead of selecting DEMO in the KEGG network provider form, enter *eco* in the organisms text input field. Make sure to select `directed network` in the KEGG network provider form, then follow steps 4 to 10 as described above.

9.2.3 Protocol for the command-line tools

The command-line version of this tutorial is restricted to the *E. coli* and *S. cerevisiae* metabolic networks. It is assumed that you have installed the required command-line tools.

1. First we construct the directed metabolic network of *E. coli*.

```
java graphtools.util.MetabolicGraphProvider -i eco -d
-o eco_metabolic_network_directed.txt
```

2. Then, we search for the lightest paths in this network as follows:

```
java graphtools.algorithms.Pathfinder
-g eco_metabolic_network_directed.txt
-f tab -s C00049 -t C00047
-r 1 -d -y con -b -T pathsUnion -O gml
-o lysinebiosyn_eco.gml
```

3. To visualize the inferred pathway, you may open lysinebiosyn_eco.gml in Cytoscape or in yED.
4. We proceed by constructing the metabolic network of *S. cerevisiae*:

```
java graphtools.util.MetabolicGraphProvider
-i sce -d -o sce_metabolic_network_directed.txt
```

5. Then, we enumerate paths between L-aspartate and L-lysine in it:

```
java graphtools.algorithms.Pathfinder
-g sce_metabolic_network_directed.txt
-f tab -s C00049
-t C00047 -d -r 1 -y con -b -T pathsUnion -O gml
-o lysinebiosyn_sce.gml
```

6. As before, we can visualize the lysinebiosyn_sce.gml file in a graph editor capable of reading gml files (such as yED or Cytoscape).

9.2.4 Interpretation of the results

After having executed the steps of this tutorial, you should have obtained two pathway images: one for the yeast network and one for the *E. coli* network. Both pathways differ quite substantially. If we compare each of these pathways with the respective organism-specific pathway map in KEGG, we notice that the pathway inferred for the *E. coli* network reproduces the reference pathway correctly.

The yeast pathway deviates from the *S. cerevisiae* KEGG pathway map from L-aspartate to but-1-ene-1,2,4-tricarboxylate, but recovers otherwise the reference pathway correctly (ignoring the intermediate steps 5-adenyl-2-amino adipate and alpha-amino adipoyl-S-acyl enzyme associated to EC number 1.2.1.31).

For comparison purposes, we have chosen the same start and end compound for both metabolic networks, but it should be noted that the reference lysine biosynthesis pathway in *S. cerevisiae* starts from 2-oxoglutarate.

The lysine biosynthesis KEGG map for yeast is available at:

http://www.genome.ad.jp/dbget-bin/get_pathway?org_name=sce&mapno=00300

The one for *E. coli* is available at:

http://www.genome.ad.jp/dbget-bin/get_pathway?org_name=eco&mapno=00300

9.3 Summary

The study case demonstrated that different organisms may employ different metabolic pathways for the synthesis or degradation of a given compound. For this reason, it is useful to be able to construct metabolic networks that are specific to a selected set of organisms.

9.4 Troubleshooting

1. An empty graph (with zero nodes and edges) is returned. Make sure that the entered organism identifiers are valid in KEGG. They should consist of three to four letters only. If in doubt, check in the provided KEGG organism list.

10 Pathway inference

10.1 Introduction

The idea of pathway inference is to connect a given set of seed nodes in the network and thereby extracting a sub-network that is optimal according to certain criteria (e.g. minimal weight or maximal relevance).

In the context of biological networks, the goal is to obtain a valid pathway for a set of biological entities of interest, e.g. genes from microarray data or compounds from metabolomic data. For instance, genes whose products participate in the same metabolic pathway are often co-expressed or grouped together in operons or regulons. We may try to reconstruct this metabolic pathway by associating the gene products to relevant reactions and connecting these reactions in a metabolic network. The resulting sub-network may be a known metabolic pathway or an unknown pathway consisting of known pathways or known reactions and compounds. In the context of microarray data, pathway inference from a set of co-expressed genes may predict which pathways are up- or down-regulated.

10.2 Inferring a pathway for a set of co-expressed genes

As an example, we take the case study discussed in [?]. In this case study, a pathway is assembled from genes in the cell-cycle regulated MET cluster [?]. Results described in this tutorial have been obtained with KEGG RPAIR version 49.0.

10.2.1 Protocol for the web server

1. In the *NeAT* menu, select the entry ***Pathwayinference***.
2. Copy-paste the gene names below in the seed nodes text field:
Met3
Met14
Met16
Met5
Met10
Met17
Met6

3. Select "Genes/Enzymes" as identifier type.
4. In the text field "Genes are from organism" type *sce*, the KEGG abbreviation for *Saccharomyces cerevisiae*.
5. Push the GO button.

The result of the mapping of the given genes to KEGG RPAIRS (reactant pairs, [?]) is displayed. Since more than one reactant pair is associated to each gene, we end up with a group of reactant pair groups. Note that each gene (except for Met5) is associated to one or more EC numbers, each of which has been mapped to its corresponding reactions in KEGG, which have in turn be mapped to their corresponding reactant pairs.

You can now select how to deal with the groups. This is a sensitive choice that strongly affects the inferred pathway and which depends on your data. In general, if you keep the original groups, you assume implicitly that only a subset of the reactions associated to the given gene will be active in the pathway. If you think that all reactions associated to a gene might be active, choose "Treat each group member as a separate group" (the default treatment).

For the study case, we recommend you to keep the default.

Push GO. In a few minutes, the result page will be displayed.

10.2.2 Protocol for the command-line tools

This section assumes that you have installed the RSAT/NeAT command line tools.

Pathwayinference is a web application that calls the pathwayinference web service. You can use the Pathwayinference command line tool on the networks provided in the network repository (check the Pathwayinference Manual for this) to reproduce results obtained with the web application on command line. Note that the mapping of genes to reactions and group treatment can only be done via the web application.

Type the following command in one line:

```
java -Xmx800m graphtools.algorithms.Pathwayinference -g RPAIRGraph_allRPAIRs_undire
-s 'RP00016#RP00182/RP00647/RP00561/RP00143#RP00960#RP04049/RP00096#RP00168#
RP04532/RP00003/RP00446/RP00946#RP00857/RP04474/RP00050#RP04533'
-f flat -b -y con -P -u -x 0.05
```

10.2.3 Interpretation of the results

The resulting sub-network contains a large part of the pathway given in [?]. Note that the chosen algorithm (kWalks in combination with Takahashi & Matsuyama) may return one from a set of solutions, so your solution may deviate from the one described here. Despite of this disadvantage, Takahashi & Matsuyama in combination with kWalks is the default algorithm, because it performed best in our evaluation. If your result deviates from the one described below, repeat the inference with the algorithm "repetitive REA".

The pathway described in the study case unites the sulfur assimilation and methionine biosynthesis pathways. It consists of the following steps:
Sulfate 2.7.7.4 Adenylyl sulfate 2.7.1.25 3'-phosphoadenylylsulfate 1.8.99.4 sulfite 1.8.1.2 sulfide (alias hydrogen sulfide) 4.2.99.10 Homocysteine 2.1.1.14 L-Methionine

The matching parts of the inferred pathway are:

RP00016 3'-Phosphoadenylyl sulfate **RP00446** Adenylyl sulfate **RP00960**
and
RP00960 Sulfite **RP00168** Hydrogen sulfide **RP01406** L-Homocysteine **RP00096**
Seeds are printed in bold.

In addition, the inferred pathway contains a branch that leads from 3'-Phosphoadenylylselenate to Adenylylselenate. This branch mirrors sulfur incorporation, but instead of sulfur, selenium is incorporated.

The presence of both the selenium and sulfur incorporation pathways in the inferred sub-network reflects the well-known fact that selenium might replace sulfur in metabolism.

This example demonstrated that given a set of differentially expressed genes from micro-array data and a metabolic network, it is possible to infer a metabolic pathway that might be affected by altered expression of the query genes.

10.3 Summary

Pathway inference allows extraction of sub-networks from larger networks given a set of seed nodes. The web application is tailored to metabolic networks, but non-metabolic networks can be processed as well.

10.4 Strengths and Weaknesses of the approach

10.4.1 Strengths

1. Sub-network extraction can be applied to any biological network.
2. It can discover unknown pathways consisting of known components.
3. It can be fine-tuned to favor certain nodes. For instance, in a global metabolic network, reactions/compounds known to occur in certain species might receive a weight much lower than other nodes, to favor extraction of species-specific sub-networks.
4. Groups of seed nodes can be specified to reflect AND/OR relationships between seeds.
5. The web application allows to infer metabolic pathways in metabolic networks extracted from the two major metabolic databases KEGG [?] and MetaCyc [?].

6. For metabolic networks from MetaCyc or KEGG, the web application supports compounds, reactions, reactant pairs, EC numbers or gene identifiers as seed nodes and handles the required mapping of these seeds to reactions, reactant pairs and compounds.
7. For metabolic networks from MetaCyc or KEGG, the web application performs a mapping of the inferred sub-network to known pathways stored MetaCyc or KEGG respectively.
8. Metabolic sub-network extraction has been validated on 71 metabolic pathways extracted from MetaCyc.

10.4.2 Weaknesses

1. In general, the accuracy of pathway inference depends on the quality of the given network and the number of seeds available.
2. Spiral-shaped metabolic pathways such as fatty acid biosynthesis can only be partly inferred.
3. In the densely connected region of metabolic networks, metabolic pathway inference cannot well distinguish alternative pathways without a large number of seed nodes.
4. The algorithms are too time-consuming to estimate p-values by computing a score distribution (where the score would be the sub-network weight) for randomly chosen seed nodes on the fly. We envisage to pre-compute these distributions for the pre-loaded networks.
5. Only one sub-network is suggested. We envisage to compute a list of them ranked by their weight.

10.5 Troubleshooting

1. Pathwayinference parameter error.
You provided insufficient or invalid parameters. Please check the pathwayinference manual page.
2. You did not specify enough valid seed node groups! Pathwayinference needs at least two valid seed node groups.
For the pre-loaded metabolic networks from KEGG and MetaCyc, each seed is mapped to data (e.g. compound/reaction identifiers, EC numbers) from these two databases. If the seeds do not map anything, they are considered to be invalid. At least two valid seed groups are needed to infer a network.
3. The node with identifier ID is not part of the input graph.
Make sure that your input network contains the node with the given identifier.

4. Pathwayinference failed to extract a subgraph.

None of the seed node groups could be connected to any other seed node group. Each might belong to a separate component of the input network or mutual exclusion (in RPAIR networks) might prevent the connection of the seed groups.

11 Recapitulative exercises